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**Question 1 continued**

Lined area for writing the answer to Question 1.

**(Total 7 marks)**

**Q1**







3. The curve  $C$  has equation

$$x = 2 \sin y.$$

(a) Show that the point  $P\left(\sqrt{2}, \frac{\pi}{4}\right)$  lies on  $C$ . (1)

(b) Show that  $\frac{dy}{dx} = \frac{1}{\sqrt{2}}$  at  $P$ . (4)

(c) Find an equation of the normal to  $C$  at  $P$ . Give your answer in the form  $y = mx + c$ , where  $m$  and  $c$  are exact constants. (4)

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**Question 3 continued**

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**(Total 9 marks)**

**Q3**

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5.

Figure 1

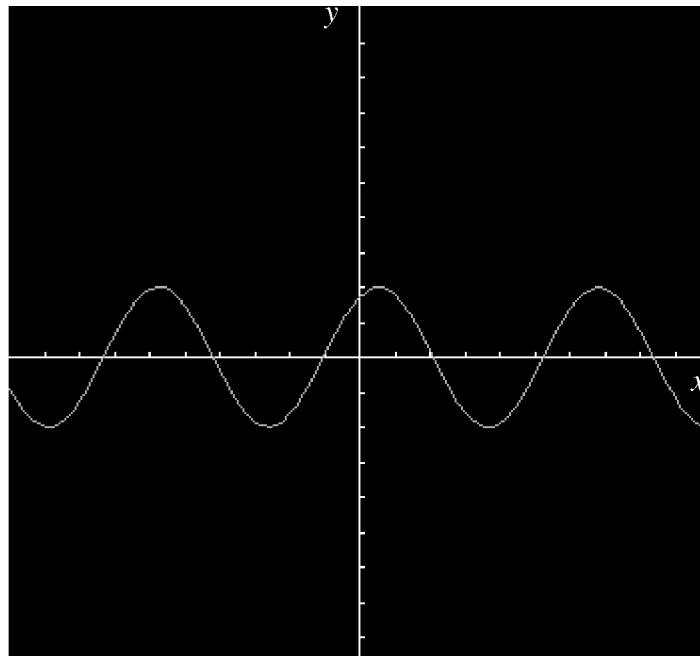


Figure 1 shows an oscilloscope screen.

The curve shown on the screen satisfies the equation

$$y = \sqrt{3} \cos x + \sin x.$$

- (a) Express the equation of the curve in the form  $y = R \sin(x + \alpha)$ , where  $R$  and  $\alpha$  are constants,  $R > 0$  and  $0 < \alpha < \frac{\pi}{2}$ . (4)

- (b) Find the values of  $x$ ,  $0 \leq x < 2\pi$ , for which  $y = 1$ . (4)

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Question 5 continued

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(Total 8 marks)

Q5

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N 2 3 5 8 3 A 0 1 3 2 4

6. The function  $f$  is defined by

$$f : x \mapsto \ln(4 - 2x), \quad x < 2 \quad \text{and} \quad x \in \mathbb{R}.$$

(a) Show that the inverse function of  $f$  is defined by

$$f^{-1} : x \mapsto 2 - \frac{1}{2}e^x$$

and write down the domain of  $f^{-1}$ .

**(4)**

(b) Write down the range of  $f^{-1}$ .

**(1)**

(c) In the space provided on page 16, sketch the graph of  $y = f^{-1}(x)$ . State the coordinates of the points of intersection with the  $x$  and  $y$  axes.

**(4)**

The graph of  $y = x + 2$  crosses the graph of  $y = f^{-1}(x)$  at  $x = k$ .

The iterative formula

$$x_{n+1} = -\frac{1}{2}e^{x_n}, \quad x_0 = -0.3$$

is used to find an approximate value for  $k$ .

(d) Calculate the values of  $x_1$  and  $x_2$ , giving your answers to 4 decimal places.

**(2)**

(e) Find the value of  $k$  to 3 decimal places.

**(2)**

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**Question 6 continued**







7.

$$f(x) = x^4 - 4x - 8.$$

- (a) Show that there is a root of  $f(x) = 0$  in the interval  $[-2, -1]$ . (3)
- (b) Find the coordinates of the turning point on the graph of  $y = f(x)$ . (3)
- (c) Given that  $f(x) = (x - 2)(x^3 + ax^2 + bx + c)$ , find the values of the constants,  $a$ ,  $b$  and  $c$ . (3)
- (d) In the space provided on page 21, sketch the graph of  $y = f(x)$ . (3)
- (e) Hence sketch the graph of  $y = |f(x)|$ . (1)

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**Question 7 continued**

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**(Total 13 marks)**

**Q7**



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21

**Turn over**



**Question 8 continued**

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N 2 3 5 8 3 A 0 2 3 2 4

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Question 8 continued

[A series of 30 horizontal lines for writing answers.]

Q8

(Total 6 marks)

TOTAL FOR PAPER: 75 MARKS

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